MODELLING THE ENERGY EXCHANGE PROCESSES BETWEEN PLANT COMMUNITIES AND ENVIRONMENT

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ABSTRACT


A steady-state, one dimensional simulation model based on the gradient diffusion approach is designed to predict the microclimate and properties of energy exchange processes between plant communities and their ambient environment. The architecture of the model is comprised of formulations of turbulent transfer, radiation distribution, and plant community energy balance. The driving forces are meteorological observations above the canopy and the necessary inputs are several geometrical, optical and ecophysiological properties of the community. The model output includes the vertical profiles of radiation, wind velocity, air and leaf temperature, humidity, source strength of heat and water vapor, and total sensible and latent heat fluxes, throughout the community. The results of simulation agree reasonably well with two sets of field measurements reported by other researchers.

INTRODUCTION

Models of energy exchange of plant communities with their environment can help plant ecologists learn more about important interactions among the plant communities, climatic conditions, soils, diseases, and insects (e.g., Waggoner, 1975; Toole et al., 1984). In addition, such models play an important role in modeling the primary production of plant communities. Such models have been developed and applied for different vegetation types (e.g., Waggoner and Reifsnyder, 1968; Stewart and Lemon, 1969; Goudriaan, 1977; Halldin and Lindroth, 1986; Wu, 1987; Wu et al., 1987).

The gradient-diffusion models use flux-gradient profile relationships, adopting a ‘first-order’ closure approach. Although the gradient-diffusion theory has been well established for the boundary layer above vegetation (Halldin and Lindroth, 1986), the validity of its application within plant communities has been questioned on several grounds (e.g., Legg and
Monteith, 1975; Raupach and Thom, 1981; Meyers, 1985). Nevertheless, the gradient-diffusion approach remains the principal foundation of modeling turbulent transfer processes above and within plant canopies (Halldin and Lindroth, 1986). Models of this sort have provided for “approximate but useful insights into the way in which physical and biological factors combine to govern the transpiration and photosynthesis rates of a plant canopy” (Raupach and Thom, 1981).

The purpose of this study is to develop and test a physically-based, mathematical simulation model of energy exchange processes and microenvironment of a herb-dominant plant community. Recent improvements in modelling of turbulent transfer processes within canopies have been incorporated. The model consists mainly of three major components: (a) radiation distribution, (b) momentum, heat, and water exchange processes, and (c) energy balance in plant communities.

DESCRIPTION OF THE MODEL *

Radiation distribution in plant communities

Solar radiation transfer. The total shortwave radiation flux density at height \( z \) in a plant community is modeled by a simple exponential formula:

\[
S_T(z) = S_{TCH} \exp[-\alpha_L \text{CLAI}(z)]
\]

where \( S_{TCH} \) is the solar radiation flux density (W m\(^{-2}\)) above the canopy, \( \alpha_L \) an empirical extinction constant ranging from 0.3 to 1.5 (Ross, 1975), and \( \text{CLAI}(z) \) the downward cumulative leaf area index above height \( z \). \( \text{CLAI}(z) \) can be related to \( \text{LAD}(z) \), leaf area density, by:

\[
\text{CLAI}(z) = \int_z^{z_{CH}} \text{LAD}(z) \, dz
\]

where the upper limit of integration \( z_{CH} \) is the average community height.

Longwave radiation transfer. The transfer of longwave radiation in plant communities is modeled through an iterative scheme as Murphy and Knoerr (1972). The total net longwave radiation exchange of a leaf layer at height \( z \) with its surroundings are expressed as:

\[
L_N(z) = V(z, S_{KY}) \sigma(T_{SK}^4 - T_L(z)^4)
+ V(z, G_{RD}) \sigma(T_G^4 - T_L(z)^4)
+ \sum V(z, X) \sigma(T_L(X)^4 - T_L(z)^4)
\]

* See Appendix.
where $\sigma$ is the Stefan–Boltzmann constant, $T_{SK}$ the apparent sky temperature, $T_G$ the ground surface temperature, and $T_L(z)$ the mean temperature of leaves in the layer at height $z$; all temperatures are expressed in kelvin.

**Total net radiation.** The total absorbed radiation $R_N$ is simply the algebraic sum of absorbed solar radiation $S_N$ and absorbed longwave radiation $L_N$ within plant communities:

$$R_N(z) = S_N(z) + L_N(z)$$  \hspace{1cm} (4)

in which absorbed shortwave radiation can be evaluated from:

$$S_N(z) = a_L S_T(z)$$  \hspace{1cm} (5)

where $a_L$ is the leaf absorptivity for solar radiation.

**Momentum, heat and water vapor exchange processes**

**Wind profile and momentum transfer.** In neutrally stratified atmosphere (i.e., where potential temperature is constant with height and vertical heat flux is zero), the vertical mean wind velocity gradient is:

$$\frac{dU}{dz} = \frac{U^*}{k(z-d)} \quad \text{for} \quad z \geq z_{CH}$$  \hspace{1cm} (6)

Integrating equation (6) yields:

$$U(z) = \frac{U^*}{k} \ln \frac{z-d}{z_0} \quad \text{for} \quad z \geq z_{CH}$$  \hspace{1cm} (7)

where $U(z)$ is the wind speed ($\text{m s}^{-1}$) at height $z$ above the canopy, $k$ is Von Karman's constant, $d$ is the zero plane displacement height (m), $z_0$ is the surface roughness length (m), and $U^*$ is the friction velocity or eddy velocity with the unit ($\text{m s}^{-1}$).

In unstable conditions (i.e., where temperature decreases with height and there exists an upward heat flux), the vertical transfer processes can be enhanced by buoyancy effect which is inversely dependent on the existing wind shear. In stable conditions (i.e., where temperature increases with height and there exists a downward heat flux), the vertical motions may be retarded somewhat. Apparently the stability of the atmosphere affects the velocity gradients, the entire wind profile, and the vertical transport processes of heat and mass.

With consideration of the buoyant effects, the wind speed gradient above a plant community can be described as:

$$\frac{dU}{dz} = \frac{U^*}{k(z-d)} \phi_m(T) \quad \text{for} \quad z \geq z_{CH}$$  \hspace{1cm} (8)
and the wind profile can be obtained by integrating (8):
\[
U(z_2) - U(z_1) = \frac{U^*}{k} \left[ \ln \frac{z_2 - d}{z_1 - d} - \Phi_m(I') + \Phi_m(I') \right]
\] (9)
in which \( \Phi_m(\Phi) \) is the stability function for momentum and \( \Phi_m(I') \) is the integrated momentum stability parameter. To solve the above equations, specifications of several parameters are required.

\( d \) and \( z_0 \) are estimated from the equations recommended by Monteith (1975) and Goudriaan (1977):
\[
\log d = 0.9793 \log z_{CH} - 0.1536 \] (10)
and
\[
\log z_0 = 0.9970 \log z_{CH} - 0.8830 \] (11)

The friction velocity, \( U^* \), is estimated from:
\[
U^* = \frac{k U(z_{RH})}{\ln[(z_{RH} - d)/z_0] - \Phi_m(I_{RH})}
\] (12)
where subscript \((RH)\) stands for the reference height.

The stability functions \( \phi_m(I') \) for momentum, \( \phi_h(I') \) for heat, and \( \phi_w(I') \) for water vapor may be expressed as (sensu Dyer, 1974; Brutsaert, 1982):
\[
\phi_h(I') = \phi_w(I') = \phi_m(I') = 1.0 \quad \text{(neutral)}
\] (13)
\[
\phi_h(I') = \phi_w(I') = \phi^2_m(I') = (1 - 16I')^{-1/2} \quad \text{(unstable)}
\] (14)
\[
\phi_h(I') = \phi_w(I') = \phi_m(I') = 1 + 5I' \quad \text{(stable)}
\] (15)
where \( I' \) is defined by
\[
I' = \frac{z - d}{L_{mo}}
\] (16)
in which \( L_{mo} \) is called Monin–Obukhov length (m), defined as:
\[
L_{mo}(z) = - \frac{\rho C_p T_A(z) U^*}{k g \text{SH}}
\] (17)
where \( \rho \) is the air density, \( g \) is the acceleration of gravity (ms\(^{-2}\)), \( C_p \) the specific heat of air (Jkg\(^{-1}\)°C\(^{-1}\)), \( T_A(z) \) the air temperature at height \( z \), and \( \text{SH} \) the sensible heat flux density (W m\(^{-2}\)).

The wind profile within plant communities is obtained from:
\[
U(z) = U(z_{CH}) \exp[\alpha_w(z/z_{CH} - 1)] \quad \text{for} \quad z \leq z_{CH}
\] (18)
where \( \alpha_w \) is the extinction coefficient.
Heat and water vapor transfer. Because of the rather small heat capacity of the air, the transfer process can be treated as a steady state case (i.e., \( \frac{dT_A}{dt} = \frac{dQ_A}{dt} = 0 \)). The profiles of air temperature and specific humidity between two arbitrary levels \( z_1 \) and \( z_2 \) above plant communities can be computed from:

\[
T_{A1} = T_{A2} + \frac{SH}{\rho C_p k U^*} \left[ \ln \frac{z_2 - d}{z_1 - d} - \Phi_h(z_2) + \Phi_h(z_1) \right] \tag{19}
\]

and

\[
Q_{A1} = Q_{A2} + \frac{LE}{\rho L_t k U^*} \left[ \ln \frac{z_2 - d}{z_1 - d} - \Phi_w(z_2) + \Phi_w(z_1) \right] \tag{20}
\]

The eddy diffusivities \( K_h \) and \( K_w \) are modeled as (Dyer, 1974; Mehlenbacher and Whitfield, 1977):

\[
K_h(z) = \frac{k U^*(z - d)}{\phi_h} \quad \text{for} \quad z \geq z_{CH} \tag{21}
\]

and

\[
K_w(z) = \frac{k U^*(z - d)}{\phi_w} \quad \text{for} \quad z \geq z_{CH} \tag{22}
\]

The steady-state vertical fluxes of sensible and latent heat within plant communities may be described by the following differential equations:

\[
\frac{dSH}{dz} = \frac{\rho C_p (T_L(z) - T_A(z)) \text{LAD}(z)}{R_h(z)} \tag{23}
\]

and

\[
\frac{dLE}{dz} = \frac{\rho L_t (Q_L(z) - Q_A(z)) \text{LAD}(z)}{R_w(z) + R_s(z)} \tag{24}
\]

The mean temperature and specific humidity profiles of air and leaves within a plant community can be predicted by solving the two second-order differential equations with specifications of the structural characteristics of the community and the turbulent diffusive properties of its ambient atmosphere.

The eddy diffusivity within canopies is modeled after Mehlenbacher and Whitfield (1977):

\[
K_h(z) = K_{hCH} \exp(\alpha_K (z/z_{CH} - 1)) \quad \text{for} \quad z < z_{CH} \tag{25}
\]

where \( K_{hCH} \) is the thermal eddy diffusivity at the canopy height, and \( \alpha_K \) is the extinction coefficient.
The leaf boundary resistance is calculated from (Gates, 1980; Paw U and Gueye, 1983):

\[ R_h(z) = C_1 \left( \frac{D_L}{U(z)} \right)^{1/2} \]  

(26)

where \( D_L \) is the average leaf dimension (m) and \( C_1 \) is a constant.

Following Mehlenbacher and Whitfield (1977), stomatal resistance profile is obtained from:

\[ R_s(z) = D_{R_Y}(z) \left( 146.0 + \frac{3.6}{4.59 \times 10^{-4} S_T(z) + 0.0015} \right) \]  

(27)

in which

\[ D_{R_Y}(z) = \frac{Q_L(z) - Q_A(z)}{Q_{crit}} \quad \text{for} \quad Q_L(z) - Q_A(z) > Q_{crit} \]  

(28)

\[ D_{R_Y}(z) = 1 \quad \text{for} \quad Q_L(z) - Q_A(z) \leq Q_{crit} \]  

(29)

where \( Q_{crit} \) is the lowest value of leaf-air specific humidity gradient affecting stomatal resistance (0.004 and 0.006 kg/kg for two different corn crops in Mehlenbacher and Whitfield's study).

**Energy balance in plant communities**

Assumed as a one-dimensional, steady-state process, the energy balance within a plant community can be described as

\[ R_N = SH + LE + G \]  

(30)

The vertical divergence equation of the energy balance can be expressed as:

\[ \frac{dR_N}{dz} = \frac{2\rho C_p}{R_h(z)} \left( T_L(z) - T_A(z) \right) \]

\[ + \frac{2\rho L_t}{R_w(z) + R_s(z)} \left( Q_L(z) - Q_A(z) \right) \]  

(31)

The profile of leaf temperature is then obtained by solving the equation:

\[ T_L(z) = T_A(z) + \frac{R_h(z)}{2\rho C_p} R_N(z) - \frac{L_t R_h(z) \left( Q_L(z) - Q_A(z) \right)}{C_p \left( R_w(z) + R_s(z) \right)} \]  

(32)

**SIMULATING SCHEME OF THE MODEL**

The basic inputs for the simulation are: (a) upper boundary conditions: the radiation, air temperature, specific humidity, and wind speed at the
reference height; (b) lower boundary conditions: the temperature and specific humidity at the soil surface; and (c) stand information: the downward cumulative leaf area index or the vertical distribution of leaf area density, the average dimension of leaves, and the average height of the plant community.

The energy balance and microenvironment within a plant community is simulated by finding a unique convergent solution for the system of equations described in the foregoing sections. Certain auxiliary formulations are needed for closing the system. Because the solutions to each of the three subsystems depends on those to the other two, the system of equations has to be solved simultaneously through successive approximations.

![Flowchart of the simulation model (PASSM)](image_url)

Fig. 1 A flow chart of the simulation model (PASSM).
The simulation model is constructed with two main loops. The loop for neutral conditions (adiabatic loop) is first iterated to convergence. The loop for stable or unstable conditions (diabatic loop) then begins iterating until the unique solution of the system of equations is found (Fig. 1). The convergence test is based upon air temperature. In most cases, only five to

Fig. 2. Profiles of measured and simulated air temperature and humidity for the S-L stand. ○, measured; ———, simulated.
ten iterations are needed for either the first or the second convergence to be reached if the allowable difference in air temperature profile between two successive computations is 0.05 or 0.01°C. The computer simulation model (PASSM) has been developed in Fortran language.

Fig. 3. Profiles of measured and simulated air temperature within and above the B–C stand. •, measured, ——, simulated.
SIMULATION RESULTS AND DISCUSSION


The simulated air temperature profiles agree well with the measurements within and above the communities (Figs. 2 and 3). The root mean square error is generally less than 0.4°C (Table 1). The modeled air humidity profiles for the S–L corn agree reasonably well with the measurements (Fig. 2). The root mean square error is 0.892 mb for August 15, and 0.672 mb for August 18 (Table 1). The major component of the error stems from the increased discrepancy near the soil surface. The simulated profiles of the air specific humidity for the B–C corn are also in reasonable agreement with the measurements, especially for the upper portion of the stands and above the stands (Fig. 4). The root mean square error for the whole profile is 0.37 mb for 9:35, 0.72 mb for 12:00, 0.50 mb for 15:05, and 0.76 for 16:02, respectively (Table 1).

From the model, the stomatal resistance curves show a reverse ‘S’ shape with two peaks (Fig. 5). The leaf-air humidity difference and the incoming solar radiation intensity are responsible for this. The warmest leaf layers in

<table>
<thead>
<tr>
<th>Time</th>
<th>Root mean square error (RMSE) a</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Air temperature</td>
</tr>
<tr>
<td></td>
<td>$T_A$ (°C)</td>
</tr>
<tr>
<td>S–L corn</td>
<td>August 15</td>
</tr>
<tr>
<td></td>
<td>August 18</td>
</tr>
<tr>
<td>B–C corn</td>
<td>09:35</td>
</tr>
<tr>
<td></td>
<td>12:00</td>
</tr>
<tr>
<td></td>
<td>15:05</td>
</tr>
<tr>
<td></td>
<td>16:02</td>
</tr>
</tbody>
</table>

a $\text{RMSE} = \left[ \frac{1}{n} \sum_{i=1}^{n} (X_{mod} - X_{meas})^2 \right]^{1/2}$

where $X_{mod}$ is the modeled value and $X_{meas}$ is the measured value.
both of the stands appear in the upper part of the communities (Fig. 6). The largest leaf-air temperature difference occurs near the canopy top, which is consistent with the observation of Brown and Covey (1966).

The measured and simulated sensible and latent heat flux densities for the S–L corn on two different days agree well with the field data (Table 2). For
the B–C corn, the simulated sensible heat flux density agrees well with the measurement, but the predicted latent flux is substantially smaller than that measured at 12:00 (Fig. 7).

The large discrepancy of the simulated air humidity in the lower part of the stands may have been caused by: (a) inaccuracy of the fitted leaf area density and the stomatal resistance; (b) sizable error from the exponential
Fig. 6. Profiles of leaf temperature for the B–C stand.

models for wind, turbulent diffusivity, and solar radiation; and (c) error in the estimated values of the lower boundary layer. The underestimate for the total latent heat flux is possibly related to the magnitude of the turbulent diffusivity, the stomatal resistance, and the aerodynamic resistance of the leaf boundary layer.
CONCLUSION

The simulated profiles of microclimatic variables generally agree reasonably well with the field measurements. Also, the modeled fluxes of heat and water vapor give good approximation for evaporation and total energy balance in a plant community. This information provides an important contribution toward understanding how plant communities interact with
TABLE 2
Comparison of measured and simulated sensible and latent heat fluxes from the S–L corn stand (W m\(^{-2}\))

<table>
<thead>
<tr>
<th></th>
<th>August 15, 1968</th>
<th>August 18, 1968</th>
</tr>
</thead>
<tbody>
<tr>
<td>Measured (^a)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>SH</td>
<td>369.9</td>
<td>376.5</td>
</tr>
<tr>
<td>LE</td>
<td>258.2</td>
<td>279.0</td>
</tr>
<tr>
<td>Simulated</td>
<td></td>
<td></td>
</tr>
<tr>
<td>SH</td>
<td>330.45</td>
<td>342.01</td>
</tr>
<tr>
<td>LE</td>
<td>240.18</td>
<td>275.60</td>
</tr>
</tbody>
</table>

\(^a\) From Stewart and Lemon (1969).

their environment and may be used toward study of the growth, survival, and reproduction of plants.

The impact of differences in turbulent diffusivity on the prediction of microclimatic profiles and total fluxes has been controversial (cf. Mehlenbacher and Whitfield, 1977; Halldin and Lindroth, 1986). In this study, it seems that the differences in the values of eddy diffusivity may affect the total fluxes of sensible and latent heat fluxes, but it tends to have much smaller impact on the profiles of air temperature and humidity.

Some aspects of the model need further improvement. First, greater accuracy of prediction of total heat and water fluxes from plant communities is needed. This may require a more comprehensive solar radiation model. Second, the discrepancy of prediction of some variables (e.g., air specific humidity) near the soil surface also requires further refinement of the model.

ACKNOWLEDGEMENTS

I am grateful to Dr. K.T. Paw U (University of California, Davis) and Dr. J.L. Vankat (Miami University, Oxford) for their guidance throughout the study. I also wish to express my appreciation for the use of computer facilities at the Department of Land, Air and Water Resources of UC-Davis and the Department of Botany of MU-Oxford.

REFERENCES


### List of Definitions and Units of Variables

<table>
<thead>
<tr>
<th>Variables and definitions</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>( a_L ) Leaf absorptivity for solar radiation</td>
<td>( \text{m}^2 \text{m}^{-3} )</td>
</tr>
<tr>
<td>( A ) Area density of plant elements</td>
<td>( \text{m}^2 \text{m}^{-3} )</td>
</tr>
<tr>
<td>( \text{CLAI} ) Downward cumulative leaf area index</td>
<td>( \text{m}^2 \text{m}^{-2} )</td>
</tr>
<tr>
<td>( C_p ) Specific heat of air: 1000.0</td>
<td>( \text{Jkg}^{-1} \text{°C}^{-1} )</td>
</tr>
<tr>
<td>( d ) Zero plane displacement height</td>
<td>( \text{m} )</td>
</tr>
<tr>
<td>( D_L ) Average dimension of leaves</td>
<td>( \text{m} )</td>
</tr>
<tr>
<td>( g ) Acceleration of gravity: 9.81</td>
<td>( \text{m} \text{s}^{-1} )</td>
</tr>
<tr>
<td>( G ) Soil heat flux density</td>
<td>( \text{Wm}^{-2} )</td>
</tr>
<tr>
<td>( k ) von Karman's constant: 0.40</td>
<td></td>
</tr>
<tr>
<td>( K_h ) Turbulent diffusivity for sensible heat</td>
<td>( \text{m}^2 \text{s}^{-1} )</td>
</tr>
<tr>
<td>( K_w ) Turbulent diffusivity for water vapor</td>
<td>( \text{m}^2 \text{s}^{-1} )</td>
</tr>
<tr>
<td>( \text{LAD} ) Leaf area density</td>
<td>( \text{m}^2 \text{m}^{-3} )</td>
</tr>
<tr>
<td>( \text{LE} ) Latent heat flux density</td>
<td>( \text{Wm}^{-2} )</td>
</tr>
<tr>
<td>( L_i ) Incoming longwave radiation</td>
<td>( \text{Wm}^{-2} )</td>
</tr>
<tr>
<td>( L_{mo} ) Monin–Obukhov length</td>
<td>( \text{m} )</td>
</tr>
<tr>
<td>( L_N ) Net longwave radiation flux density</td>
<td>( \text{Wm}^{-2} )</td>
</tr>
<tr>
<td>( L_i ) Latent heat of vaporization of water</td>
<td>( \text{Jkg}^{-1} )</td>
</tr>
<tr>
<td>( Q_A ) Specific humidity of air</td>
<td>( \text{kgkg}^{-1} )</td>
</tr>
<tr>
<td>( Q_L ) Specific humidity of leaves</td>
<td>( \text{kgkg}^{-1} )</td>
</tr>
<tr>
<td>( R_h ) Leaf boundary-layer resistance for sensible heat transfer</td>
<td>( \text{s} \text{m}^{-1} )</td>
</tr>
<tr>
<td>( R_N ) Total net radiation</td>
<td>( \text{Wm}^{-2} )</td>
</tr>
<tr>
<td>( R_s ) Stomatal resistance for water vapor</td>
<td>( \text{s} \text{m}^{-1} )</td>
</tr>
<tr>
<td>( R_w ) Leaf boundary-layer resistance for latent heat transfer</td>
<td>( \text{s} \text{m}^{-1} )</td>
</tr>
<tr>
<td>( \text{SH} ) Sensible heat flux density</td>
<td>( \text{Wm}^{-2} )</td>
</tr>
<tr>
<td>( S_N ) Net solar radiation flux density</td>
<td>( \text{Wm}^{-2} )</td>
</tr>
<tr>
<td>( S_T ) Total solar radiation</td>
<td>( \text{Wm}^{-2} )</td>
</tr>
<tr>
<td>( T_A ) Actual air temperature</td>
<td>( \text{°C} )</td>
</tr>
<tr>
<td>( T_G ) Soil surface temperature</td>
<td>( \text{°C} )</td>
</tr>
</tbody>
</table>
\( T_L \) Leaf temperature \( °C \)
\( T_{SK} \) Apparent sky temperature \( °C \)
\( U \) Wind velocity \( m s^{-1} \)
\( U^* \) Friction velocity \( m s^{-1} \)
\( V \) View factor
\( z \) Vertical distance from the soil surface \( m \)
\( z_0 \) Roughness length \( m \)
\( z_{CH} \) Average height of a plant community \( m \)
\( \alpha_k \) Extinction coefficient for eddy diffusivity
\( \alpha_L \) Radiation extinction coefficient by leaves
\( \alpha_w \) Extinction coefficient for wind velocity
\( \Gamma \) Stability parameter, defined by \((z - d)/L_{mo}\)
\( \rho \) Air density \( kg\,m^{-3} \)
\( \sigma \) Stefan-Boltzmann constant: \( 5.57 \times 10^{-8} \) \( W\,m^{-2}\,K^{-4} \)
\( \phi_h \) Stability function for heat
\( \phi_m \) Stability function for momentum
\( \phi_w \) Stability function for water vapor
\( \Phi_h \) Integrated stability parameter for heat
\( \Phi_m \) Integrated stability parameter for momentum
\( \Phi_w \) Integrated stability parameter for water vapor

**Subscripts**

A Air
CH Plant community height
h Sensible heat
L Leaf
m Momentum
N Net
RH Reference height
w Water vapor